Melting points of water models: Current situation

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ABSTRACT

By using the direct coexistence method, we have calculated the melting points of ice I_h at normal pressure for three recently proposed water models, namely, TIP3P-FB, TIP4P-FB, and TIP4P-D. We obtained $T_m = 216$ K for TIP3P-FB, $T_m = 242$ K for TIP4P-FB, and $T_m = 247$ K for TIP4P-D. We revisited the melting point of TIP4P/2005 and TIP5P obtaining $T_m = 250$ and 274 K, respectively. We summarize the current situation of the melting point of ice I_h for a number of water models and conclude that no model is yet able to simultaneously reproduce the melting temperature of ice I_h and the temperature of the maximum in density at room pressure. This probably points toward our both still incomplete knowledge of the potential energy surface of water and the necessity of incorporating nuclear quantum effects to describe both properties simultaneously.

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When simulating water, a force field is needed and it is common to use a simple rigid non-polarizable force field. Usually, positive charges are located on the hydrogen atoms and a Lennard-Jones center is located on the oxygen. In three center (3C) models, the negative charge is located on the oxygen atom as in the TIP3P,¹ SPC,² and SPC/E (Extended Simple Point Charge Model),³ models proposed by the groups of Jorgensen and Berendsen, respectively. In the four center (4C) models the negative charge is located along the bisector of the H-O-H angle,⁴ leading to the popular TIP4P model.¹ In this first wave of water models (1980s), the density and vaporization enthalpy were used as target properties (although in the case of SPC/E only when including the self-energy correction³). Water, at constant pressure, has a temperature at which the density reaches a maximum (TMD). Recognizing the importance of that led to the second wave (2000-2010) of potential models where the TMD was used as a target property. Two different approaches to achieve this goal were used. In the first approach, the negative charge was located in the position of the lone pair electrons as in the TIP5P⁵ (a geometry also used in the old ST2 model⁶), resulting in five center (5C) models. In the second approach, the TIP4P geometry was kept, but the vaporization enthalpy was sacrificed as a target property (unless the self-energy correction is included) in favor of the TMD as in the TIP4P-Ew⁷ and TIP4P/2005 models.⁸ Over the last

ten years, some additional non-polarizable models have been proposed, some of them using a 3C geometry as OPC-39 or TIP3P-FB¹⁰ and some of them using a 4C geometry as TIP4P-FB,¹⁰ TIP4P- ϵ ,¹¹ TIP4P-D,12 or OPC (Optimal Point Charge Water Model).13 In general, the aim of these models was to improve the description of the dielectric constant of liquid water (but not in ices) with respect to TIP4P-Ew and TIP4P/2005 models although, in general, the improvement was made at the cost of deteriorating the predictions for another property (see Ref. 14 for a general discussion on the role of the dielectric constant in water simulations). If we focus on polarizable models, we can also find three new and interesting force fields, such as the BK3,¹⁵ i-AMOEBA,¹⁶ and MB-Pol¹⁷ or HBP (Hydrogen-Bonding Polarizable)¹⁸ models, which add polarization to a 4C geometry. The TMD (at 1 bar) is not only an interesting property of water but also the melting point of ice I_h (also at 1 bar). In fact, one of the properties that one can study to validate a water force field is the melting point of ice I_h . For most of the models proposed up to 2012, the melting point of ice is well known.^{19,20} For some of the models proposed over the last ten years, we know now the melting point, as, for instance, for OPC and OPC-3²¹ and for TIP4P- ϵ .¹¹ However, the melting point of ice I_h for three popular recently proposed water models, namely, TIP3P-FB,¹⁰ TIP4P-FB,¹⁰ and TIP4P-D,¹² is unknown. The goal of this work is to determine their melting temperatures and to summarize the current situation of force fields with respect to their capacity to predict the melting point of ice and the TMD.²² We will use the direct coexistence method¹⁹ where a solid phase consisting of 2000 molecules of ice I_h (proton disordered configuration was obtained using the algorithm of Buch et al.²³) is placed in contact with 2000 molecules of liquid water. The ice plane exposed at the interface is the secondary prismatic one (1210). We have performed anisotropic NpT simulations with the GROMACS package²⁴ with a time step of 2 fs. Temperature and pressure were kept constant by using the Nosé-Hoover thermostat²⁵ and Parrinello-Rahman barostat²⁶ both with a coupling constant of 2 ps. For electrostatics and Van der Waals interactions, the cut-off radii was fixed at 1.0 nm and long-range corrections to the Lennard-Jones (LJ) part of the potential in the energy and pressure were applied. We used PME (Particle Mesh ewald)²⁷ to account for the long-range electrostatic forces and LINCS²⁸ for constraints.

In Fig. 1, the time evolution of the potential energy of the system at several temperatures for TIP4P-FB and TIP4P-D force fields is shown. For the TIP4P-FB model, ice melts (i.e., energy grows) for all temperatures above 243 K. Ice grows at all temperatures below 241 K. Thus, we can conclude that the melting temperature for the TIP4P-FB model is $T_m = 242(1)$ K (not surprisingly similar to that of TIP4P/ ϵ $T_m = 240(1)$ K, taking into account the similarity of the parameters of both models). Following the same procedure, we estimate that the melting temperature of the TIP4P-D force field is $T_m = 247(1)$ K. To evaluate the impact of the cutoff on the calculations, we repeated for TIP4P-D the calculations using a larger cutoff (i.e., 1.2 nm) obtaining again $T_m = 247(1)$ K.

We have also recalculated the melting point of TIP4P/2005 and TIP5P using the same system size obtaining 250(1) and 274(1) K, respectively (see the supplementary material). The melting point of TIP4P/2005 is in excellent agreement with the result reported by Conde *et al.*²⁹ Finally, we also evaluated the melting point of



FIG. 1. Evolution of the potential energy as a function of time for the NpT runs of TIP4P-D (top) and TIP4P-FB (bottom) models at 1 bar and different temperatures. The energies of the TIP4P-D water model are shifted 1.3 kcal/mol for better visualization of the reader.

TIP3P-FB obtaining (see the supplementary material) $T_m = 216(4)$ K (the larger error bar is due to the slow dynamics at such low temperatures). We have also determined the melting enthalpy at the melting temperature for TIP3P-FB, TIP4P-FB, OPC, TIP4P-D, and TIP5P obtaining 0.63, 0.99, 1.07, 1.11, and 1.78 kcal/mol, respectively, compared with the result obtained for TIP4P-2005 (i.e., 1.13 kcal/mol) and the experimental value (i.e., 1.44 kcal/mol). Let us now present a more general discussion. In Fig. 2, the results of the melting point of water models are presented. In Table I, we also show the numerical results for the melting points, the TMD of the models, and the difference in temperature between the TMD and the melting temperature $(\Delta T = TMD - T_m)$. As can be seen in Fig. 2, 3C models yield a poor description of the melting temperature of ice I_h (the average being located around 220 K). In short, 3C models are not recommended to study the freezing of water (in addition, ice I_h may not be the most stable phase at room pressure for these models³⁰). 4C models improve the description, the average melting temperature being around 245 K. As can be seen, the melting points of TIP4P-FB and TIP4P-D are below that of TIP4P/2005. Polarizable models using a TIP4P geometry improve the description of the melting point, the average being located around 255 K but still below the experimental value. The only models reproducing the experimental value are those of the 5C geometry, the coarse grained mW,³¹ the TIP6P-Ew,³² and the special purpose model TIP4P/Ice.33 In general, the melting point increases with the value of the quadrupole moment of the model.34

It is interesting to analyze the performance of the models with respect to the TMD. In Fig. 2, models with a small deviation (4 K or less from the experimental value) are represented as blue squares, models with a moderate deviation (i.e., between 5 and 10 K) are represented by empty squares, and models with a large deviation from experiment (more than 10 K) are represented by black squares. As can be seen, models that reproduce well the melting point do not reproduce well the TMD and vice versa. For most of the models, the difference in temperature between the TMD and the melting



FIG. 2. Melting points of ice I_h of different water models at 1 bar. Blue filled squares: models that provide (at 1 bar) a good estimation of the TMD (maximum of 4 K of deviation from the experiment). Empty squares: models that provide a fair estimation of the TMD (maximum of 5–10 K of deviation from the experiment). Black filled squares: models with a bad estimation of the TMD (more than 10 K deviation from the experiment).

Model	T _m (K)	TMD (K)	ΔT (K)
Expt.	273	277	4
TIP3P	$146(5)^{20}$	182 ³⁵	36
SPC	$190.5(5)^{20}$	228 ³⁵	37.5
SPC/E	$214(3)^{19}$	241 ³⁵	27
TIP3P-FB	216(4) this work	261 ¹⁰	45
$SPC-\epsilon$	$230(2)^{36}$	270 ³⁶	40
$SPC-\epsilon_1$	$220(2)^{36}$	250 ³⁶	30
OPC-3	$210(10)^{21}$	260 ⁹	50
TIP4P	$229(9)^{37}$	253 ³⁵	24
TIP4P-FQ	303(8) ³⁸	280 ³⁹	-23
TIP4P-Ew	$241(1)^{19}$	274 ⁷	33
TIP4P-2005	250(1) this work	277 ⁴⁰	27
TIP4P-ice	$270(3)^{19,29}$	295 ³⁵	25
OPC	$242.2(0.9)^{21}$	272 ¹³	29.8
TIP4P- ϵ	$240(2)^{11}$	276 ¹¹	36
TIP4P-FB	242(1) this work	277 ¹⁰	35
TIP4P-D	247(1) this work	270 ¹²	23
TIP5P	274(1) this work	284.5 ^{22,41}	10.5
TIP5P-Ew	$271(3)^{19}$	282 ⁴²	11
ST2	$299(2)^{43}$	323 ⁴⁴	24
TIP6P-Ew	$274.5(1.5)^{32}$	290 ³²	15.5
mW	$273(1.5)^{45}$	251 ⁴⁵	-22
i-AMOEBA	$261(2)^{16}$	277 ¹⁶	16
BK3	$250(3)^{15}$	275 ¹⁵	25
MB-Pol	$263.5(1.5)^{17}$	263 ⁴⁶	-0.5
HBP	247(3) ¹⁸	254 ¹⁸	7

temperature is too large, ranging from 11 to 50 K, when compared to the experimental value that is only 4° (the only exceptions are the MB-Pol and HBP models for which this difference is almost 0 and 7 K, respectively).

To summarize, in this work, we have determined the melting points of three recently proposed rigid and non–polarizable water models (TIP4P-FB, TIP4P-D, and TIP3P-FB) with the goal of analyzing if they could reproduce simultaneously the melting point and the TMD. The answer is negative and their melting points are similar (although a few degrees lower) than that of TIP4P/2005. The main conclusion is that in 2022, we do not have yet any model of water (polarizable or not) able to reproduce simultaneously both the melting point of ice I_h and the TMD. Further work is needed to determine whether this is a deficiency in the description of the potential energy surface (PES) of water of all force fields proposed so far, or to the necessity of incorporating nuclear quantum effects to describe both properties at the same time accurately.^{47–49} If this were the case, then even an accurate PES could not reproduce both properties simultaneously when using classical simulations.

See the supplementary material for additional figures of the melting point of the models studied in this work and for the compar-

ison of different properties, such as melting enthalpy and densities of ice and liquid water for each model.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

NOTE

DATA AVAILABILITY

The data that support the findings of this study are available within the article and its supplementary material.

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